

i.e. Derivation of gas law's

$$PV = \text{Constant}$$

$$\text{or } P \propto \frac{1}{V} \text{ at constant Temperature } T$$

This is Boyle's law

2. Derivation of Charles' Law from Kinetic Gas Equation.

We know,

$$PV = \frac{2}{3} RT$$

$$\text{or } V = \frac{2}{3} \frac{R \cdot T}{P}$$

$$V = \frac{2R}{3P} \cdot T$$

If Pressure  $P$  is constant,

then  $V \propto T$

3. Avagadro's Law Derivation:-

When two gases have the same Pressure and Volume,  
then  $P_1 V_1 = P_2 V_2$

We know from Kinetic gas eq<sup>n</sup>  $PV = \frac{1}{3} m n c^2$

Applying Kinetic gas eq<sup>n</sup>

$$\frac{1}{3} m_1 n_1 c_1^2 = \frac{1}{3} m_2 n_2 c_2^2$$

$$\frac{2}{3} \cdot \frac{1}{2} m_1 n_1 c_1^2 = \frac{2}{3} \cdot \frac{1}{2} m_2 n_2 c_2^2$$

$$\text{or } \frac{1}{2} m_1 n_1 c_1^2 = \frac{1}{2} m_2 n_2 c_2^2 \quad \text{--- (1)}$$

When the temperature of these two gases is also the same,  
then their Kinetic energy per mole will also be the same

$$\text{i.e. } \frac{1}{2} m_1 c_1^2 = \frac{1}{2} m_2 c_2^2 \quad \text{--- (2)}$$

Dividing equation (1) by (2)

$$\text{we get, } n_1 = n_2$$

Thus the equal volumes of all gases under the same conditions of temperature and Pressure have the same number of moles. This is Avagadro's Law.

(4) Graham's Law of Diffusion: -

If  $M$  is the total mass of a gas, then the Kinetic gas equation,

$$PV = \frac{1}{3} mnc^2, \text{ reduces to -}$$

$$PV = \frac{1}{3} Mc^2$$

$$\text{or } c^2 = \frac{3PV}{M} = \frac{3P}{\frac{M}{V}} = \frac{3P}{D} \quad \left[ \frac{M}{V} = \text{Density} \right]$$

$$\text{or } c^2 = \frac{3P}{D}$$

$$c = \sqrt{\frac{3P}{D}} \quad \text{--- (1)}$$

Where  $D$  is the density of the gas, we know that the rate of diffusion ( $r$ ) of a gas varies with the mean velocity ( $c$ ),  $(\because r = \frac{c}{4})$

from the above eqn (1)

$$c \propto \sqrt{\frac{1}{D}} \quad \text{where } P \text{ is constant}$$

Thus the rate of diffusion of a gas is inversely proportional to the square root of density of the gas at constant pressure.

This is the Graham's law of diffusion.

5) Dalton's Law of Partial Pressure: -

If  $n_1$  molecules each of mass  $m_1$  of a gas A are taken in a container of volume  $V$ . Then the pressure  $P_a$  for the gas is given by Kinetic gas eqn

$$P_a = \frac{m_1 n_1 c_1^2}{3V}$$

Similarly for gas B,

$$P_b = \frac{m_2 n_2 c_2^2}{3V}$$

If both the gases are present in  $3V$  the same containers, then total

Pressure,

$$P = \frac{m_1 n_1 c_1^2}{3V} + \frac{m_2 n_2 c_2^2}{3V}$$

$$= P_a + P_b$$

Similarly for  $n$  gases, the total pressure,

$$P = P_a + P_b + P_c + \dots + P_n$$

This is Dalton's Law of Partial Pressure.